

1 **Reviewer 2:** We thank reviewer 2 for their positive comments and appreciate the helpful errata spotted. We agree the  
2 "Additional feedback" discussion is beyond the scope but look forward to having this important discussion.

3 **Reviewer 3: "So in summary, the point of the paper is the improve runtime with an approximate algorithm."**  
4 We strongly disagree with this casting, and the hope that the reviewer might reconsider in light of our comments.  
5 Improving runtime is not the key focus of the paper. There currently exists no algorithm to compute MCR for random  
6 forests whatsoever (and so nothing to improve runtime or accuracy over!). The approximations made in the technique  
7 we introduce are there so that calculation of MCR across a Rashomon set of RF models is physically tractable for the  
8 first time (along with accompanying proofs). This is the key contribution.

9 **"The primary problem I have with this paper is that it does not compare with a good baseline.":** We also disagree  
10 with this statement. The suggested MCR+ "rough equivalent" is inherently flawed and does not provide a sound measure  
11 of the upper bound of a variable when interactions exist amongst the input variables. E.g, in the synthetic XOR example  
12 each variable by itself predicts no better than chance, the same as a constant predictor. Therefore, the "rough equivalent  
13 MCR+" would return all zeros where the known truth is all 0.5 (see paper Fig 1). A method to measure upper bounds of  
14 variable importances in real world situations, which typically do contain variable interactions, is a key contribution of  
15 the work. More subtly the suggested MCR- baseline, hold-one-out VI, also does not offer a MCR baseline. As we note  
16 (although clearly opaquely) on lines 92-94 algorithm reliance methods (holding out variables) are not only a function  
17 of models that fit the data well while MCR methods are. The meaning and implication of this difference and why it  
18 matters (and therefore why hold-one-out should not be an MCR baseline) is strongly made in Fisher et al.'s (paper  
19 [7]) establishment of MCR in their 60-page JML paper both theoretically (§3.2) and empirically (§9.1). While a full  
20 discussion remains outside of the scope of this paper, given length constraints, we propose the inclusion of a slightly  
21 longer description of their argument to make it clearer why this should not be considered a baseline.

22 **Reviewer 4 and 5 question whether the found "equivalent" models will retain the same predictive performance**  
23 **on new data as the reference model (RM), i.e. remain in the  $\epsilon$ -Rashomon set around the RM as we tend to the**  
24 **population.** We agree this is an extremely interesting issue. However, the proposed method is based (inc. proofs  
25 and empirical evidence for MCR convergence) on constructing  $\epsilon$ -Rashomon sets ( $\epsilon$ -sets) based on in-sample (fit)  
26 equivalence. As correctly pointed out by the reviewers, making the claim that one can find  $\epsilon$ -sets based on generalized  
27 performance equivalence would require significantly more theoretical and empirical investigations. Its inclusion, in  
28 addition to developing and evaluating the proposed approach, however would take the work well beyond the length and  
29 scope possible in a NeurIPS paper. Therefore, we wish to note: (1) in general this is an open problem for MCR with  
30 Fisher et. al not fully addressing this issue but rather providing a proof (valid for our work) that in-sample estimation is  
31 sufficient under large sample sizes and a reference model with correctly selected complexity (their §4.1). (2) What is  
32 proposed corresponds to the real world use case where MCR would be computed based on a reference model trained  
33 on the full dataset as part of a fit(via CV to determine model complexity)-refit(on full data) methodology to model  
34 building. Notably, this is the underpinning use-case when the use of training data is motivated (instead of a test set)  
35 for computing traditional permutation importance (c.f. Interpretable Machine Learning by Molnar, 2020). (3) While  
36 we realise that our technique focuses on fit  $\epsilon$ -sets equivalence that we strongly believe this still makes an important  
37 statistical contribution in the road towards MCR. We thank the reviewers for highlighting this need for clarity and the  
38 importance of this discussion. We will include this clarification and discussion if accepted.

39 **Reviewer 4 suggests the inclusion of (1) an ablation experiment to understand the importance of the two steps**  
40 **(2) further simulation studies** With regard to (1) we have these results, as we did examined them ourselves, and simply  
41 left them out due to space. If accepted we will inject these as part of our additional page allowance. In brief: surrogates  
42 account for a change in the permutation importance by 0-13% while the majority (remainder) of the change comes  
43 from the second transform. With regards to (2), further simulation studies were run as part of the work and we agree  
44 that these provide additional insights. However, we feel that their inclusion would not provide significant additional  
45 insight worthy of the removal of other analysis/points given the available space. Finally, with respect to boosted trees -  
46 developing an MCR method for this class is of interest and part of our future work and something we're interested in  
47 discussing. Unfortunately, the approach does not directly transfer and is outside the scope of this work.

48 **Reviewer 5:** We agree the comparison to SHAP is not entirely fair. Line 90-92 attempts to indicate this. We are happy  
49 to adjust/extend the wording to clarify the use case differences between SHAP and MCR. With regard to the discussion  
50 of the cancer results: The fact that MCR- is 0 for all variables indicates that, there is at least one model in the Rashomon  
51 set (set of equally performant models) that does not rely on this variable to make predictions (although other models do,  
52 as indicated by the non-zero MCR+) and that the set is non-trivially large. Therefore, in certain contexts, i.e. when  
53 fitting a model and undertaking VIM to consider potential causal factors, fitting a single model would not provide the  
54 full picture. We agree, however, that in some cases (as mentioned in the introduction) this doesn't matter. If accepted  
55 we will briefly extend the discussion of the cancer results to ensure the interpretation is clear. We thank Reviewer 5  
56 (as with all other reviewers) for the additional errata and pointing out lines requiring minor clarification (i.e. line 273)  
57 which we agree to.