

1 **Author Feedback:** Mostly, we would like to address Reviewer #4 who has misunderstood virtually
 2 all parts of our paper. First, Reviewer #4 claims that our paper only works for orthogonal tensors. This
 3 is not true and is actually the main point of the paper. As we discussed at length in Section 1.1 the
 4 only previous works *with provable guarantees* needed to assume orthogonality, near orthogonality
 5 or used a very large semidefinite program. We use PCA in each iteration, but as we explained, the
 6 goal is to find an approximation to the subspace spanned by the unknown factors (whether they be
 7 orthonormal or not) and then in a postprocessing step that works via Jennrich’s algorithm to find
 8 factors that span this space that work (but again, they need not be orthonormal).

9 Second, Reviewer #4 has seemingly missed the entire point of the paper that the goal is to provide
 10 the first theoretical guarantees for exact tensor completion (and as a bonus we get a practical new
 11 algorithm). Instead Reviewer #4 opines that we sacrifice the monotone improvement property of
 12 ALS. So? ALS has no known provable guarantees and as we show experimentally can get stuck in
 13 suboptimal local minima. Instead we give a new method that provably works and achieves linear
 14 convergence rate and never gets stuck. The goal of our paper is to discover new ways to do things.
 15 These involve subtle changes and Reviewer #4 has seemingly misunderstood how our algorithm
 16 works and instead attempts to draw faulty analogies with other existing methods.

17 Third, Reviewer #4 makes some bizarre claims, such as arguing that the $r > n$ case is the most
 18 interesting and natural setting. Tensor decompositions and completions are used in practice in many
 19 applications tensors are at least close to being low rank. In fact a google search for the exact phrase
 20 "Low Rank Tensor Completion" yields over 35k results.

21 That said Reviewer #4 brings up a fair point that we could have included more experimental com-
 22 parisons, e.g. with other heuristics that are out there that do not have provable guarantees. First, as
 23 has been documented many times in the literature (see [1]), standard baselines (ADMM, FaLRTC,
 24 TMac, TTN) that require storing the whole tensor in memory run out of memory even on tensors that
 25 have dimensions $15000 \times 15000 \times 5$. These tensors have about as many entries as the tensors in our
 26 largest experiments. Second we tried out the CPD method in tensorlab which indeed performs much
 27 worse than our method. For example, when we have a random tensor with $n = 200$, $r = 4$ and the
 28 number of observations is 50000 our method reliably achieves very small 10^{-6} error whereas CPD
 29 reliably achieves error rates that are orders of magnitude worse, between 10^{-1} and 10^0 . Only when
 30 the number of observations is much larger (200000) does CPD start to be competitive.

	Kronecker Comp. (50k)	Tensorlab CPD (50k)	Kronecker Comp. (200k)	Tensorlab CPD (200k)
$10^{-1} < \text{err} < 10^0$	1	36	0	10
$10^{-2} < \text{err} < 10^{-1}$	0	4	0	5
$10^{-6} < \text{err} < 10^{-2}$	1	0	0	2
$\text{err} < 10^{-6}$	38	0	40	23

Figure 1: Entries are the number of trials out of 40 that achieved a certain relative RMSE. Kronecker Comp. (our algorithm) is run for 100 iterations. Tensorlab CPD is run with all default settings.

32 Reviewer #3 asks about the relation between our work and the paper “Provable tensor factorization
 33 with missing data”. In fact, they assume that the factors are orthogonal. In contrast, ours is the first
 34 algorithm to achieve exact recovery while allowing the factors to be strongly correlated.

35 Reviewer #1 asks about the complexity of the LS step. The LS problem we are solving involves
 36 $r^{O(1)}$ variables and so it can be straightforwardly solved in nearly linear time in the number of
 37 observations (when r is polylogarithmic) using Gram-Schmidt. We will clarify this in our paper. The
 38 only important point is that, while the vectors have dimension n^2 , they are sparse so we just need to
 39 store their nonzero entries as lists.

40 Reviewer #1 also asks about how to set the parameters in practice. We can always terminate the
 41 iterative step early if we reach small enough error. The important thing is how the parameters in
 42 Theorem 3.2 should be set, and we find that in practice changing the 300 in the exponent to 2 suffices.
 43 Our focus was the dependence of our sample complexity and running time on n , but seemingly it
 44 does quite well in terms of r too, which is necessary for the kinds of experimental results we get.

45 [1] Xiawei Guo, Quanming Yao, and James Tin-Yau Kwok. Efficient sparse low-rank tensor
 46 completion using the frank-wolfe algorithm. In *Thirty-First AAAI Conference on Artificial
 47 Intelligence*, 2017.