

1 We thank the reviewers’ time and energy for reading our paper and providing all these comments and suggestions.
2 We are also appreciative for the positive feedback, including that this work has “solid/important theoretical results”
3 (R2/R5), “meticulous, thorough” development of the graphical characterization (R4), and the complete algorithm that
4 “looks inspiring” (R3). Below, we address some of the concerns raised by the reviewers.

5 **Comparison to (Kocaoglu et al., 2019) [14] (R2).** We provide a detailed comparison of our work to that of [14] in
6 Appendix D.3. Unfortunately, we could not include this material in the main paper due to the lack of space. In short, we
7 consider the problem of learning from interventional data with *unknown interventional targets*, a setting which cannot
8 be handled by the work in [14]. When considering the results in [14], we make the following contributions:

- 9 1. We formulate the Ψ -Markov property and derive a graphical characterization that subsumes that of [14], which is
10 formally shown in Proposition 7, Appendix D.3.
- 11 2. We show that the algorithm introduced in [14] is not applicable under unknown interventional targets and present a
12 complete algorithm (Ψ -FCI) under unknown interventional targets (Example 10).
- 13 3. We handle causal sufficiency as a special case of the derived results. Subsection 3.1 establishes a graphical
14 characterization for this case, and Section C, in the Appendix, presents an algorithm for learning an equivalence
15 class from interventional data under causal sufficiency. We prove this algorithm to be complete for both known and
16 unknown interventional targets. The work in [14] does not discuss the causally sufficient case nor completeness.

17 **C-faithfulness versus Faithfulness (R2 & R5).** As noted by R2, c-faithfulness is indeed stronger than the faithfulness
18 assumption, which is common for learning Markov equivalence classes from when only data from one distribution, the
19 observational one is available. A similar assumption is also required in other works [10, 18, 32, 14], but it is phrased
20 slightly differently depending on the specific setting. The preliminary experimental results in Appendix D suggest
21 that c-faithfulness largely holds, especially in the discrete case. However, we do understand the concern of R2 that
22 c-faithfulness may not hold in some settings, in a similar fashion as the faithfulness assumption in the observational case.
23 The present work provides necessary conditions to establish the theoretical limitations of inferring causal invariances
24 from the combination of multiple datasets, and it paves the way for heuristic and approximation algorithms that may
25 weaken the c-faithfulness assumption, akin to weakening faithfulness in the observational case (e.g., Zhalama, Zhang,
26 J., Mayer, W. (2017). Weakening faithfulness: some heuristic causal discovery algorithms. *JDCA*, 3(2), pp. 93-104).

27 **Further Empirical Evaluation (R4 & R5).** We agree that additional experiments would be helpful to refine the
28 theoretical understanding under finite samples and other empirical constraints. In this spirit, we have conducted
29 experiments on Sachs data [26] after the submission. We indeed observe discrepancies in the recovered structures
30 compared to JCI [18]. We will provide and discuss these findings in relation with the known ground truth. We also
31 conducted synthetic experiments with two other generating causal graphs (Fig.1(a) and Fig.4(a) with discussions in
32 Ex.6 and Ex.8, respectively) and the results look similar to the ones we included in the paper (Fig.6(a)). For the camera
33 ready, we will conduct more synthetic experiments on random causal graphs and include the results.

34 **Theorem 4 in the Appendix (R4).** Thm. 4 establishes that a tuple of distributions that is generated by a causal
35 graph satisfies the Ψ -Markov property relative to the graph and the true set of interventional targets (lines 174-176).
36 This ascertains that the equivalence class learned by Ψ -FCI is non-empty (Theorem 2), i.e., the equivalence class is
37 guaranteed to include at least the generating causal graph and the true unknown set of interventional targets. We will
38 make this point more prominent by referencing the theorem in the main text (instead of only the section, line 176).

39 **Testing the Distributional Invariances (R5).** There are different ways of implementing hypothesis testing for the
40 distributional invariances discussed in line 22 of Ψ -FCI, which can be seen as evaluating statements like $|\hat{P}_i(y|w) -$
41 $\hat{P}_j(y|w)| \leq \epsilon$, where the hat represents the empirical distribution. Ψ -FCI is agnostic to the particular implementation of
42 the test, which is in general chosen based on the specific details of the setting. Still, for concreteness, when the support
43 of two distributions $\hat{P}_i(y, w)$ and $\hat{P}_j(y, w)$ is the same, testing whether $\hat{P}_i(y|w)$ is equal to $\hat{P}_j(y|w)$ can be done as
44 follows. First, define a binary variable F which is set to 0 for a sample from i and set to 1 for a sample from j . Then,
45 test if $I(F; Y|W)$ is zero. In our experiments, we use the previous method to test the distributional invariances.

46 **Hard Interventions (R5).** The presented characterization and algorithm are sound under hard interventions; however,
47 the equivalence class can be further refined in this setting due to the change in the adjacencies of the graphical model
48 following from the do-intervention. To understand the subtlety, consider the graphs $\mathcal{G} = \{X \rightarrow Y\}$, $\mathcal{D} = \{X \leftarrow Y\}$ and
49 $\mathcal{I} = \langle \{X\}, \{Y\} \rangle$. The pairs $\langle \mathcal{G}, \mathcal{I} \rangle$ and $\langle \mathcal{D}, \mathcal{I} \rangle$ are Ψ -Markov equivalent according to Thm. 1. However, the graphs
50 are distinguishable under hard interventions since $(X \not\perp\!\!\!\perp Y)_{\mathcal{G}_{\bar{X}}}$ while $(X \perp\!\!\!\perp Y)_{\mathcal{D}_{\bar{X}}}$. Given this realization, we opted to
51 avoid discussing hard interventions since the results are somewhat direct but much weaker.

52 **Comparison to (Rothenhäusler et al., 2015) [25] (R5).** We briefly mentioned this work in the introduction, lines
53 68-69. We ended up not doing a detailed comparison to Ψ -FCI given the very nature of both approaches, they are not
54 really comparable. On the one hand, [25] considers the broader class of cyclic causal models while ours is restricted to
55 acyclic models. On the other hand, our work makes no assumption about the functional form or type of soft intervention,
56 while [25] considers linear causal relations and shift interventions. We will reflect this discussion in the paper.