

1 We thank the reviewers for their constructive feedback. **We have reformulated the theoretical statements to position**  
 2 **them with previous work, clarified notation and surface-level inconsistencies in theoretical statements, added**  
 3 **experiment baselines, and performed an additional comparison with SPIBB (Laroche et al. 2019).** The main  
 4 contribution of our work is a *practical* offline deep RL algorithm, CQL, which attains strong results and outperforms  
 5 prior methods by a large margin on a wide range of tasks. We have revised the paper to frame the theoretical results as  
 6 providing motivation for our approach rather than a primary contribution.

7 **Additional experiments & baselines:** Fu et al. (2020) have added results for AWR, BCQ, REM and AlgaeDICE in  
 8 the D4RL paper, which we now include in Tables 1 & 2. We have added an explicit mention that the baseline numbers  
 9 are from Fu et al. 2020 [R2, (R3, W4)] and will add variance measurements [R2]. CQL outperforms AWR, BCQ,  
 10 REM and AlgaeDICE (R1) in 26/29 tasks, often by a large margin. (R3) We also compared CQL to SPIBB on the  
 11 Helicopter task from Laroche et al. 2019. With a dataset of size 10k, CQL outperforms SPIBB by attaining 4.11 mean  
 12 return whereas SPIBB (w/ best  $N_\lambda$ ) attains 3.22 return and soft-SPIBB (w/ best  $\epsilon$ ) attains 3.65 return.

13 **R1/[R3, W1]: Policy improvement result, what is CQL doing.** Based on R1/R3’s requests, we have added a new  
 14 theorem for policy improvement property of CQL that is more consistent with prior work. Similar to Thm. 1 in Laroche  
 15 et al. 2019, we show that the CQL updates (Eqn. 2) converge to the optimal policy of a (empirical) penalized RL  
 16 objective, i.e.,  $\pi_{\text{CQL}} = \arg \max_{\pi} \hat{J}_{\mathcal{D}}(\pi) - \alpha \mathbb{E}_{\mathbf{s} \sim \hat{d}_{\pi}} [D_{\text{CQL}}(\pi, \pi_{\beta})] (1 - \gamma)^{-1}$ , where  $\hat{J}_{\mathcal{D}}(\pi)$  is an empirical estimate of  
 17 expected discounted return and  $D_{\text{CQL}}$ , defined in lines 649-650, captures a notion of action distribution shift. Then,  
 18 using the terminology from Laroche et al. 2019, we show that  $\pi_{\text{CQL}}$  is a  $\zeta$ -approximate safe policy improvement over  
 19  $\pi_{\beta}$  (i.e.  $J(\pi_{\text{CQL}}) \geq J(\pi_{\beta}) - \zeta$ ) with high probability  $1 - \delta$ , where

$$\zeta = \frac{\gamma C \sqrt{\log(1/\delta)}}{(1 - \gamma)^2} \mathbb{E}_{\mathbf{s} \sim \hat{d}^{\pi_{\text{CQL}}(\mathbf{s})}} \left[ \frac{\sqrt{|\mathcal{A}|}}{\sqrt{|\mathcal{D}(\mathbf{s})|}} \sqrt{D_{\text{CQL}}(\pi_{\text{CQL}}, \pi_{\beta})(\mathbf{s}) + 1} \right] - \frac{\alpha \mathbb{E}_{\mathbf{s} \sim \hat{d}^{\pi_{\text{CQL}}(\mathbf{s})}} [D_{\text{CQL}}(\pi_{\text{CQL}}, \pi_{\beta})(\mathbf{s})] (1 - \gamma)^{-1}}{\left( \hat{J}_{\mathcal{D}}(\pi_{\text{CQL}}) - \hat{J}_{\mathcal{D}}(\pi_{\beta}) \right)} .$$

20 This follows from applying and extending the tools in Achiam et al. 2017. Note the similarity with Thm. 2 in (Laroche  
 21 et al. 2019) and that we avoid the  $\infty$ -norm term in (Petrik et al. 2016). Intuitively, this indicates that the return of  
 22  $\pi_{\text{CQL}}$  is higher than the behavior policy  $\pi_{\beta}$  w.h.p. when the empirical policy improvement (i.e., the  $\alpha$  term) exceeds the  
 23 sampling error, which diminishes to 0 as the dataset size (i.e.,  $|\mathcal{D}(\mathbf{s})|$ ) grows.

24 **R2: Behavior policy estimation.** Since our submission, Nair et al. 2020 and Ghasemipour et al. 2020 have discussed  
 25 the difficulty of behavior policy estimation at length. We will add extended discussion of this point in the paper.

26 **R1/(R3, W2): Clarifying notation and resolving surface level inconsistencies.** We have resolved the notational  
 27 confusion and inconsistencies in the results. We discuss the main changes briefly:

- 28 - (Also R3, C5) We now explicitly indicate dimensions of vectors, matrices and scalars. Briefly,  $[\mu(\mathbf{a}|\mathbf{s})/\pi_{\beta}(\mathbf{a}|\mathbf{s})]$   
 29 denotes a vector of size  $|\mathcal{S}||\mathcal{A}|$  equal to elementwise ratio of  $\mu$  and  $\pi_{\beta}$  and this is multiplied to the matrix  $(I - \gamma P^{\pi})^{-1}$ .
- 30 - (Also R3, C1)  $\pi_{\beta}(\mathbf{a}|\mathbf{s}) = 0$ : We have added a discussion to indicate that when  $\pi_{\beta}(\mathbf{a}|\mathbf{s})$  is zero in the tabular setting,  
 31 the learned Q-values,  $\hat{Q}(\mathbf{s}, \mathbf{a})$  can be  $-\infty$ . For Thm 3.1 and 3.2, we have edited these to include the assumption that  
 32  $\pi_{\beta}(\mathbf{a}|\mathbf{s})$  has non-zero density on all actions to prevent  $-\infty$  values, and clarified that this result holds only for  $\mathbf{s} \in \mathcal{D}$ .

33 **R1/[R3, C3]: Tightened bounds with counts.** For simplicity, we had omitted the count terms from the main text,  
 34 instead deferring discussion to App. D.3. However, as the reviewers point out, they are necessary. We now include the  
 35 count terms that scale inversely proportional to the square root of  $|\mathcal{D}(\mathbf{s}, \mathbf{a})|$  in the main text. As expected, the sampling  
 36 error and theoretically safe value of  $\alpha$  both decrease as the dataset size increases. In practice, the theoretical value of  $\alpha$   
 37 is overly-conservative, so as done in previous work, we use a smaller  $\alpha$  rather than this theoretical value.

38 **(R3, W3): Relation to prior work.** We have added and positioned our ideas with respect to the suggested references  
 39 on robust MDPs, CPI, safe PI, high confidence PI, batch RL (Also R1), including 12 references from non-Alphabet  
 40 authors. We suspect that CQL outperforms robust MDPs empirically due to the approximations necessary to adapt  
 41 robust MDPs to a practical algorithm. We have also added an empirical comparison to SPIBB.

42 **R1/[R3, C2]: Offline RL and state distribution shift.** We have clarified these statements (e.g., lines 83-84) to say  
 43 that *training procedure* for a Q-learning algorithm queries out-of-distribution actions which can lead to divergence.

44 **(R3, C4): Lines 847-848: no guarantee  $(s', a') \in \mathcal{D}$ ?** To clarify, the proof uses concentration of  $\hat{T}(\cdot|\mathbf{s}, \mathbf{a})$  which  
 45 depends on the counts  $|\mathcal{D}(\mathbf{s}, \mathbf{a})|$ . So while the inequalities involve  $(s', a')$  through  $\mathbb{E}[\hat{Q}^k(s', a')]$ , we bound that term by  
 46  $2R_{\max}(1 - \gamma)^{-1}$  avoiding concerns over the size of  $|\mathcal{D}(s', a')|$ . We explicitly mention this now.

47 **R1: Intuition for gap expanding.** We have elaborated on this in the paper now. By increasing the difference between  
 48 Q-values at in-distribution actions ( $\pi_{\beta}$ ) and under learned policy ( $\mu_k$ ), CQL constrains the resulting policy to lie in  
 49 the support of  $\mathcal{D}$ . This controls the  $D_{\text{CQL}}(\pi, \pi_{\beta})$  term that appears in the sampling error component of  $\zeta$  in our  $\zeta$ -safe  
 50 policy improvement result above. Empirically, this also makes CQL more robust to Q-function approx. error that makes  
 51 OOD actions appear more optimal and results in better performance than policy constraint methods (App. B, Fig. 2).