

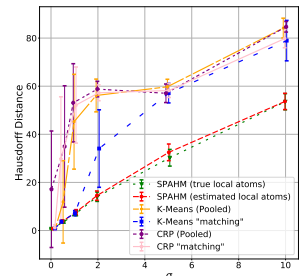
1 We thank the reviewers for their time, their valuable and encouraging feedback, and their recommendations for
2 improvement. We remain confident that our work is of strong interest to the NeurIPS community and easily can
3 incorporate the suggested changes in a revision for the conference. Answers to specific comments appear below.

4 **Related literature.** We thank **R1** and **R2** for pointing at several related papers. We believe that our model and
5 inference techniques are substantially different, however we agree that all of the mentioned papers are relevant. We
6 present a brief discussion below and we will add an extended discussion (and citations) to our paper.

7 **R1** suggested that Local Partition Process (LPP) of Dunson (2009) allows for sharing a subset of coordinates, which
8 may be beneficial. We note that LPP is applied in a regression-like problem where there is a *single* global parameter - a
9 vector of regression coefficients, and each dataset selects a (sparse) subset of the coordinates of this vector. In our work
10 there is a *collection* of global parameters and each dataset selects an (also sparse) subset of these global parameters
11 via the Bernoulli process, i.e. Q_j . On a high level, both models perform a sparse subset selection, however there are
12 significant differences in modeling goals and inference. We suspect it might be possible to apply our model in the
13 problem studied by Dunson and apply LPP in our setting, however it remains to be seen whether inference with LPPs
14 can be generalized to the local models with inherent *permutation invariance* (mixtures, HMMs, etc.) that we consider.
15 To clarify, in Dunson (2009), regression coefficients are naturally aligned across datasets as they are ordered according
16 to the data coordinates; in our work, mixture components may be ordered arbitrarily for each dataset. What is perhaps
17 a more worthy direction for future work is to develop a model capable of *both* selecting from a collection of global
18 parameters and their coordinates.

19 **R2** mentioned a series of papers studying *meta-analysis of Bayesian analyses* applicable to random effects, linear
20 regression, and other similar models. The key difference in our work is that we consider models with inherent
21 *permutation invariant* structure of the parameter space: we demonstrate examples with mixtures, topic models, HMMs,
22 and sparse GPs. Permutation invariance leads to inferential challenges associated with finding correspondences across
23 sets of local parameters and learning the size of the global model, which are addressed in our work. On the other hand,
24 it is not clear how the approach of Dutta et al. (2016) can be applied to models such as mixtures. The work of Heikkilä
25 et al. (2017) and Blomstedt et al. (2019) have similar modeling limitations, however they suggest interesting directions
26 for future work: how to strengthen privacy preserving properties of SPAHM to guarantee *differential privacy* as in
27 former, and how to generalize SPAHM to aggregate *local posteriors* instead of parameters as in the latter.

28 **Baselines.** **R3** asked for comparison to stochastic variational inference (SVI). In the
29 paper we do compare against (memoized) online variational inference (see line 274)
30 for the HDP-HMM models, which is the state-of-the-art for inference in such models
31 and outperforms SVI. We also compare against a Gibbs sampler (line 245) for the
32 Gaussian topic models. In both cases, SPAHM either outperforms or performs comparably
33 while being significantly faster. Here, using SVI for inference, we compare to Chinese
34 Restaurant process (CRP) in simulations as requested by **R1**. We also compare to
35 CRP fitted with local centroid estimates, alike meta-modeling suggested by **R2**. This
36 experiment is an extension of the Figure 1 of our paper. CRP performance is similar to
37 k-means (which is expected as we have been fitting k-means with true L in our experiments) and is inferior to SPAHM.



38 **R2**, if we understood correctly, suggested we compare to a full Bayesian hierarchical model and to other meta-modeling
39 approaches to illustrate why our method is necessary. We believe that such results are contained in the paper. For
40 example, in the Gaussian topic models experiment SPAHM is over 1400 times faster than hierarchical model inference
41 with a Gibbs sampler (see lines 247-248). For the meta-modeling, we considered k-means clustering of the *local*
42 *parameters* as a basic baseline: SPAHM outperforms this baseline in the motion capture experiment (see Fig. 4 left and
43 lines 291-298) and in simulation studies (see k-means “matching” in Figures 1 and 2). In the figure presented in this
44 rebuttal we also considered CRP “matching” as another meta-modeling baseline approach.

45 **Model and inference clarifications.** **R1** asked about the data partitions — we assume that local datasets (and
46 corresponding parameters) are independently but *not* identically distributed. For example, our method can aggregate
47 topics learned from datasets generated with *different* numbers of topics and even different topic models.

48 **R3** asked about learning the cardinality of C_j and parallelizing the algorithm. It is important to clarify that our approach
49 performs *meta-modeling*. This means that first each dataset is processed independently and *in parallel* to obtain
50 local sets of parameters. For a dataset j , there are $\text{card}(C_j)$ parameters, where $\text{card}(C_j)$ may be a hyperparameter
51 or can be learned by applying an appropriate Bayesian nonparametric model *locally*, as we’ve done in our motion
52 capture experiment. Then, these parameters serve as *input* to our algorithm and are not being updated. Our algorithm
53 non-parametrically learns the global set of parameters and its size, allowing for data privacy and significant speedups
54 compared to full Bayesian hierarchical learning (e.g., in the topic modeling experiment, our method is 1400 times faster
55 than full hierarchical inference - see lines 247-248).