

1 Dear reviewers, we would first like to thank you for the helpful comments and suggestions of improvements. Remarks
 2 concerning typos, bad notations and missing references will be fixed according to your suggestions if the manuscript is
 3 accepted. Please see our detailed answer to your major concerns below:

4 **Computational aspects:** The implementation described
 5 in the paper corresponds to a naive one, that computes dis-
 6 tances matrices along the projections, and is not the most
 7 efficient. Pykeops was used to avoid memory overflows in
 8 the evaluation of the cost in Eq (3) which was computed
 9 in $O(n^2)$ (both space and time). In fact this implemen-
 10 tation was unnecessary since the final cost can actually
 11 be computed in $O(n \log(n))$. Indeed, one can develop
 12 the sum (3) to compute it in $O(n)$ operations: the term
 13 depending on σ (Eq (2)) can be computed in $O(n)$ oper-
 14 ations using $W(x, y, \sigma)$ as shown in the supplementary
 15 material and for the remaining constants $\sum_{i,j} (x_i - x_j)^4$
 16 (idem for y) the binomial development gets rid of the
 17 $\sum_{i,j}$ and only involves \sum_i terms that can be computed
 18 in $O(n)$ operations. Overall, in 1D, GW can be com-
 19 puted as efficiently as Wasserstein. As a consequence,
 20 the complexity of SGW is exactly the same as for Sliced
 21 Wasserstein and Pykeops is not needed anymore. We believe this discussion can be added without changing the overall
 22 message of the paper by updating Fig 3 using a pure pytorch implementation as in Fig 1. With this implementation, one
 23 can compute SGW between 1M point distributions in 1s (vs 100s with a naive PyKeops implementation). Note also that
 24 entropic-GW is implemented on GPU as well. This way, it is clear that our method is responsible for the computational
 25 gain that **is not a consequence of using PyKeops (#R1)**.

26 Related to the remark of (#R1) we also added the runtimes for two different numbers of projections $L = 50, 200$. The
 27 paragraph "Computational aspects" of the paper describes the influence of L on the theoretical complexity. To the
 28 best of our knowledge, the effect of L on the quality of estimation of the expectation is a hard question that is still
 29 open for the Sliced Wasserstein itself. Runtimes are computed between 2D measures since the dimension does not
 30 have an impact on the complexities for computing GW and SGW (they only depend on L and n) (#R1). Moreover,
 31 the optimization over the Stiefel manifold does not depend on the number of points but only on the dimension d of
 32 the problem so that overall complexity is $n \text{ iter} (Ln \log(n) + d^3)$, which is affordable for small d . On the spirals we
 33 observed that computing RISGW is one order of magnitude slower than the non-RI variant on CPU, which is still
 34 reasonable (# R1). We propose to add this discussion in the manuscript.

35 The non Hilbertian case is a very good remark (#R3). One straightforward approach would be to consider an embedding
 36 of the distances using multi-dimensional scaling as a preprocessing step or to learn distance-preserving embeddings
 37 using Siamese networks. This would come with an additional cost but we believe that this direction is worth investigating
 38 and will add it to the discussion.

39 **About the choice of Δ :** The map Δ is one of the contributions of the paper. Here we propose a simple method (using
 40 a linear map in the Stiefel manifold) to align the spaces, even though one could consider other approaches (e.g a Δ
 41 parameterized by a neural network). We believe designing Δ is application dependant and preferred to restrict Δ to the
 42 Stiefel manifold in order to ensure rotation invariant guarantees so as to make the connection with an important property
 43 of GW. As such, we can use the Δ formulation when $p = q$ to recover this property (#R1). We thank (#R4) for its
 44 remark concerning the 4 others discrepancies. We originally did not want to add non obvious extensions of W, SW using
 45 the " Δ trick" and only focus our paper on Gromov-Wasserstein as our main result is Theo 3.1. We believe that using Δ
 46 with other discrepancies deserves a deeper study since it raises a lot of quantitative and theoretical questions (e.g closed
 47 forms for Δ) and we chose not to include such discussions in the scope of the paper. From a purely computational point
 48 of view, complexity of all methods are the same (cf remark above). Nevertheless we will add these discrepancies and
 49 run corresponding experiments with them in the supplementary as suggested by the reviewer.

50 **Theoretical aspects and proofs:** (#R1) the problem (3) is equivalent to Eq (2) in 1D since the quadratic term is constant
 51 w.r.t. the permutation σ (as being of the form $\sum_{i,j} c_{\sigma(i),\sigma(j)} = \sum_{i,j} c_{i,j}$) so that the minimization only involves the
 52 cross products. We will clarify this point.

53 **Experiments:** (# R1) The idea behind the simple spiral example was just to illustrate the different behaviors of GW,
 54 SGW and RISGW w.r.t rotations. Indeed, other rotation invariant methods could be applied here and would give similar
 55 results.

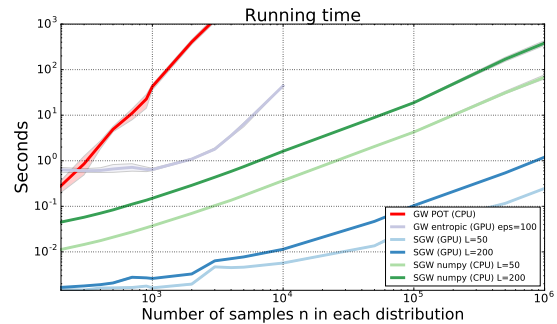


Figure 1: Runtimes comparison between SGW, GW, entropic-GW between 2D random distributions with varying number of points from 0 to 10^6 in log-log scale