

1 We thank the reviewers for their positive feedback and constructive comments. We will summarize and respond to the  
2 comments of all the reviewers. All reviewers recognize our contributions as 1) being among the first to design flows for  
3 discrete data, 2) building a bridge between generative flow models and compression. The reviewers see the topic of  
4 discrete flows as emerging and important. Moreover, the reviewers agree that the paper is easy to read, clearly organized  
5 and that the experiments are well chosen and demonstrate the compression capability of the proposed model. Reviewer  
6 2 thinks that our paper will be used by others.

7 Reviewer 1 and 2 refer to concurrent work on discrete flows by Tran et al., which is acknowledged in both our paper  
8 and theirs. Although there are clear similarities between the two approaches, i.e. both works use the straight-through  
9 estimator, we focus on the use of discrete flows for ordinal data and explore connections between generative modelling  
10 and data compression, whereas Tran et al. focus on nominal data and perform experiments in an NLP setting.

11 Reviewer 2 indicates that she/he is unsure if we have implemented an actual encoder-decoder pair. We want to emphasize  
12 that this is in fact the case. The encoder is defined by the forward pass of the IDF flow model and the rANS encoder,  
13 whereas the decoder consists of the rANS decoder and the inverse of the IDF. Hence, the combination of our IDF and  
14 the rANS encoder are a direct replacement for conventional methods such as JPEG2000 or PNG. In addition, the results  
15 presented in Table 2 are the *actual* compression rates obtained using the IDF + rANS encoder-decoder, given both as  
16 bits per dimension (bpd) in the bitstream and compression rate.

17 Reviewer 3 is of the opinion that it is preferable to compare the proposed model to existing flow methods in terms of  
18 their generative performance. It is argued that we should compare samples from our model at higher resolutions (e.g.  
19 64x64 or 96x96 etc), and that the negative log likelihood (NLL) results are only reported on low-resolution datasets. We  
20 would like to emphasize that table 3 includes NLL results on the 64x64 version of ImageNet. Hence we disagree with  
21 the statement that we do not consider datasets with large enough images to be able to judge the generative modeling  
22 performance from the NLL scores. However, we agree that the samples shown in figure 7 of our model trained on  
23 ImageNet 32x32 are depicted too small. We will fix this by showing a smaller number of samples of an IDF model that  
24 was trained on ImageNet 64x64.

25 Last but foremost, we stress that our main goal is to design a flow-based lossless compression algorithm for discrete  
26 ordinal data such as images. We have demonstrated that our results are state-of-the art on this task in table 1 and 2. We  
27 consider the task of generative modeling (results in table 3) as complementary.

28 Reviewer 2 would like to see a more elaborate discussion of the design choices in our model, such as the dependency  
29 structure in the prior and the use of a discretized logistic prior. An intuitive argument for the dependency structure in  
30 the prior is that it provides a natural ordering for the partial loading of a data stream as depicted in Figure 8. Note that  
31 this type of structured prior is also used in Glow. A discretized logistic is preferred over a softmax prior because 1) a  
32 softmax prior does not model the ordinality among discrete variables, as opposed to the discretized logistic; 2) IDF  
33 can output any integer when mapping an image to latent space, even integers  $<0$  and  $>255$ . It is therefore not trivial  
34 to implement a categorical distribution using a softmax for this type of support. In contrast, a discretized logistic has  
35 infinite support by design making it a more natural choice. 3) A softmax prior is more expensive in terms of the number  
36 of parameters than a (mixture) of discretized logistic distributions. Each logistic distribution is determined by only 2  
37 parameters. The number of required mixture components is not high either (we use only 5 in our paper).

38 As for the differences in the models in table 3 (mentioned by reviewer 2): we took Glow as a starting point for the  
39 architecture design, and replaced the ResNets in the coupling layers with DenseNets. For ImageNet32, RealNVP uses  
40 less parameters than IDF and its continuous version (CF) ( $46.2M^1$  vs  $58.5M$ ), whereas IDF/CF is more efficient in the  
41 case of ImageNet64 ( $84.3M$  vs  $184.9M^1$ ). To reduce the effect of the bias from the straight through estimator for the  
42 rounding operator we use fewer but more complex coupling layers as compared to Glow (See discussion section 4.1).  
43 The second difference lies in the use of additive (translation) coupling layers, as opposed to affine (translation + scale  
44 layers). However, we'd like to point out that Kingma & Dhariwal (2018) experimentally showed that the difference  
45 between affine and additive coupling layers is fairly small. We have purposely included results for the continuous  
46 version of IDF, such that comparing it with IDF on the one hand and RealNVP/Glow/Flow++ on the other hand allows  
47 to distinguish the influence of discretization and architecture design. We hope this sufficiently addresses reviewer 2's  
48 questions on the comparison between models in table 3.

49 Finally, reviewer 3 questions how the determinant of the Jacobian matrix is computed for the continuous generalization  
50 of our model. The continuous version is obtained from IDF by removing the rounding operator. It therefore still only  
51 contains translation/additive couplings, leading to a Jacobian determinant of one.

52 Again, we thank the reviewers for their positive and constructive feedback. We hope that we have sufficiently addressed  
53 the remaining questions/comments of the reviewers, and we will incorporate the above clarifications into the final  
54 version of our paper.

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<sup>1</sup>This number was obtained from the implementation released by Google